Membrane Adhesion via Homophilic Saccharide-Saccharide Interactions Investigated by Neutron Scattering

Emanuel Schneck, † Bruno Demé, ‡ Christian Gege, § and Motomu Tanaka *•
† Physical Chemistry of Biosystems, Institute of Physical Chemistry, University of Heidelberg, Heidelberg, Germany; ‡ Institut Laue-Langevin, Grenoble, France; § Department of Chemistry, University of Konstanz, Konstanz, Germany; and • Cell Biophysics Lab, Institute of Toxicology and Genetics, Karlsruhe Institute of Technology, Karlsruhe, Germany

ABSTRACT Solid-supported membrane multilayers doped with membrane-anchored oligosaccharides bearing the LewisX motif (LeX lipid) were utilized as a model system of membrane adhesion mediated via homophilic carbohydrate-carbohydrate interactions. Specular and off-specular neutron scattering in bulk aqueous electrolytes allowed us to study multilayer structure and membrane mechanics at full hydration at various Ca²⁺ concentrations, indicating that membrane-anchored LeX cross-links the adjacent membranes. To estimate forces and energies required for cross-linking, we theoretically modeled the interactions between phospholipid membranes and compared this model with our experimental results on membranes doped with LeX lipids. We demonstrated that the bending rigidity, extracted from the off-specular scattering signals, is not significantly influenced by the molar fraction of LeX lipids, while the vertical compression modulus (and thus the intermembrane confinement) increases with the molar fraction of LeX lipids.

INTRODUCTION

Cell-surface glycans in the form of glycolipids, glycoproteins, and glycocalix polysaccharides (1) serve not only as stabilizers for the integrity of cell membranes but also as specific ligands to communicate with neighboring cells. Although most of the receptors for cell-surface carbohydrates are proteins (e.g., lectins (2,3)), there are several examples of specific interactions between complementary carbohydrate motifs (4,5). For example, the homophilic interactions of membrane-bound saccharides bearing the neutral LewisX (LeX) trisaccharide motif

\[ D-\text{Gal}\beta(1\rightarrow4)[L-\text{Fuc} \alpha(1\rightarrow3)]D-\text{GlcNAc}\beta(1\rightarrow R) \]

were reported to play key roles in the aggregation of cells during the embryonic development (6,7). Although the capability of carbohydrate-carbohydrate interactions to induce cell aggregation was demonstrated by in vitro studies, it has been difficult to quantify such interactions that are weaker than carbohydrate-protein interactions. There have been several approaches to establish model systems to study the carbohydrate-carbohydrate interactions on the molecular level. For example, Geyer and co-workers (8,9) incorporated LeX lipids in planar micelles (called bicells) for NMR spectroscopy. Hernández et al. (10) coupled LeX via alkylthiolate to Au nanoparticles and Si₃N₄ tips coated with Au and studied the interactions with planar Au substrates functionalized with LeX thiol using surface plasmon resonance and atomic force microscopy (5), respectively. Gourier et al. (11) incorporated LeX lipids into giant vesicles and measured the adhesion energy using micropipette aspiration.

In contrast to other high-resolution probing methods (e.g., scanning and electron microscopy), x-ray and neutron scattering is not limited to free surfaces, but has also access to buried structures. Ricoult et al. (12) carried out small-angle x-ray scattering and small-angle neutron scattering experiments to determine the influence of lactitol glycolipids on the interaction of charged DDAB membranes, which only form stable multilayers under high osmotic pressures. McIntosh and Simon (13) incorporated GM1 glycolipids into egg-PC membrane multilayers and reported that the contribution of the saccharides to the membrane interactions is purely repulsive.

While scattering from isotropic suspensions generally does not allow for the distinct determination of structures parallel and perpendicular to the membrane planes, planar sample geometries enable one to identify specular and off-specular scattering signals (14–16). To date, this method has been commonly used for the physical characterization of planar stacks of phospholipid membranes using x-rays and neutrons (17–21).

In our previous accounts, we have demonstrated the potential of this technique to determine structure and mechanics of planar membrane stacks of synthetic glycolipids and bacterial lipopolysaccharides (22,23). In this study, we prepared stacks of planar phospholipid membranes incorporating lipids with LeX headgroups (LeX lipids). To shed light on the role of saccharide-saccharide interactions in membrane adhesion processes, we studied the influence of specific LeX-LeX pairs on the structural ordering and mechanics of the membranes in aqueous buffers using specular and off-specular neutron scattering.
Simulation of the scattering signals based on mechanical parameters

Realistic sets of membrane-displacement correlation functions were modeled in a continuum approximation based on the discrete smectic Hamiltonian (14). Within this framework, the vertical compressibility of the membrane stacks is characterized by the compression modulus $B$, whereas the resistance of the membranes against bending is characterized by the membrane bending modulus $\kappa$. The membrane-displacement correlation functions $g_k(r)$ can be expressed with the Caillé parameter $\eta$ and the De Gennes parameter $\lambda$ of smectic liquid crystals (14) (see Eq. 2). Here, $k = 0$ corresponds to the membrane self-correlation and $k > 0$ to the cross-correlations of the membranes with their $k^{th}$ neighbors. The value $r$ denotes the in-plane distance between two points. As shown in our previous article (23), the effect of the finite sample size can be taken into account with an effective cut-off radius $R$, which coincides with an upper limit for the wavelength of the membrane fluctuations. Mathematically, $R$ defines a lower integration limit in the calculation of the correlation functions,

$$g_k(r) = \frac{d^2}{\pi^2} \frac{\eta}{A^2} \int_{2\pi/k}\left[1 - J_0(q_{\parallel} r) \exp(-\lambda k q_{\parallel}^2 d)\right] dq_{\parallel}, \quad (2)$$

where

$$\eta = \frac{\pi k_B T}{2d^2 \sqrt{\kappa B/d}}$$

and

$$\lambda = \frac{\sqrt{\kappa}}{Bd}$$

For known lamellar periodicities $d$, the correlation functions are fully determined by the three free parameters $\eta$, $\lambda$, and $R$. The scattering signals were modeled in kinematic approximation, which requires that the intensity of the scattered beam is much weaker than the incident illumination. To guarantee the validity of this assumption, only the second Bragg sheets, whose intensity nowhere becomes comparable to the incident intensity, were considered. In kinematic approximation, the scattering from periodical membrane stacks can be expressed (23,27) as a function of the membrane displacement correlation functions $g_k(r)$:

$$S\left(q_{\parallel}, q_{\perp}\right) \propto \frac{1}{q_{\perp}^2} \left[ N \int_{-\infty}^{\infty} e^{-q_{\parallel}^2 \tau_0(r)/2} \exp\left(i q_{\parallel} r\right) dr + 2 \sum_{k=1}^{N} (N - k) \cos(k q_{\parallel} d) \int_{-\infty}^{\infty} e^{-q_{\parallel}^2 \tau_0(r)/2} \exp\left(i q_{\parallel} r\right) dr \right]. \quad (3)$$

Based on this expression, which includes specular and diffuse contributions, the scattering signals were modeled in the angular coordinates of the experiment to maintain a uniform grid of points both in experimental and simulated datasets. Instrumental resolution was included by convolution of the

**FIGURE 1** Chemical structure of the synthetic LeX lipid.
signal in Ω- and Γ-directions with Gaussian functions, representing the point spread function of the measurement resulting from the finite angular width and the wavelength spread of the neutron beam. The convolution in Ω-direction was achieved using the Fourier convolution theorem in the computation of the Fourier integrals in Eq. 3, while the convolution in Γ-direction was applied to the simulated intensity maps. In the simulations, η, λ, and B were varied to minimize deviations from the experimental results for 1), the Γ-integrated Bragg sheet intensity and 2) the Γ-width of the sheets simultaneously. Subsequently, κ and B were calculated from η and λ.

**Modeling of intermembrane interaction forces**

**DPPC membranes in Ca\(^{2+}\)-free buffer**

The interaction of neutral DPPC membranes in L\(_a\)-phase in Ca\(^{2+}\)-free buffer was modeled considering three force contributions and a suited definition of the membrane separation \(d_{\text{w}}\).

1. van der Waals (vdW) forces. For lipid membranes, several models have been developed (28,29). To account for the van der Waals attraction between the phospholipid membranes in fluid L\(_a\) phase, we used the “double film model” from Demé et al. (30) with one Hamaker constant \(A = 5.1 \times 10^{-21}\) J. The value \(d_{\text{w}}\) is defined as the lamellar periodicity \(d\) minus the hydrophobic membrane thickness \(d_H\). For the lipids with dihexadeyl chains (DPPC and Le\(^X\) lipid) studied here, \(d_{\text{w}}\) was estimated referring to the corresponding value reported by Janiak et al. (31) for DMPC with ditetradecyl chains (\(d_{\text{w}} = 35.5\) Å). By adding four times the average projected length of a hydrocarbon C-C bond in L\(_a\) phase membranes (0.8 Å) (32), we obtained \(d_{\text{w}} = 38.7\) Å.

2. Hydration repulsion. This force obeys an exponential decay (33) characterized by the extrapolated pressure \(P_\text{E}\) at \(d_{\text{w}} = 0\) and a decay length \(\lambda_{\text{HYP}}\). We used the values reported by Demé et al. (30), \(\lambda_{\text{HYP}} = 2.0\) Å and \(P_\text{E} = 4.5 \times 10^{10}\) Pa.

3. Undulation repulsion. This interaction was modeled according to the classical expression derived by Helfrich (34,35):

\[
\Pi_{\text{UND}}(d_{\text{w}}) = \alpha_\text{w} \left(\frac{k_B T}{d_{\text{w}}}\right)^2 - \frac{2}{kd_{\text{w}}}. \tag{4}
\]

Here, \(d_{\text{w}}\) was defined as the periodicity \(d\) minus the steric thickness, \(d_s\). For DPPC membranes in L\(_a\)-phase, we used the value reported by Kucerka et al. (36), \(d_s = 45.9\) Å.

In our calculations, the prefactor \(\alpha_\text{w} = 0.10\) was taken according to the results obtained using Monte Carlo simulations (37,38), and we used the bending rigidity that we measured for DPPC membranes at 60°C, \(\kappa = 18\ k_B T\) (see Fig. S1 and Table S1 in the Supporting Material).

The correct description of undulation interactions in membrane stacks is still under debate (39). Despite the notion that the strength of the undulation repulsion is correlated to the other interfacial forces, accurate treatments explicitly accounting for this interplay are still missing. An approach by Evans and Parsegian (40) resulted in an overestimation of the repulsion strength. To date, Helfrich’s classical treatment has been most successful in reproducing experimental data (39,41). In this study, we compared the results to alternative calculations using \(\alpha_\text{w} = 0\) and \(\alpha_\text{w} = 0.23\) (Helfrich’s original estimate), and confirmed that our general conclusions are independent of the exact choice of \(\alpha_\text{w}\) within this interval.

**DPPC membranes in Ca\(^{2+}\)-loaded buffer**

Several studies have reported that the presence of Ca\(^{2+}\) ions significantly increases the lamellar periodicity of phospholipid membranes (42,43). Deuteron magnetic resonance experiments have evidenced the binding of Ca\(^{2+}\) to phosphatidylcholine headgroups (44). This would alter the net charge of the membrane from neutral to positive, resulting in electrostatic repulsions. Therefore, electrostatic repulsion has to be considered in the theoretical modeling of force balance to reveal the effect of Ca\(^{2+}\). For this purpose, the Ca\(^{2+}\) ions adsorbed to the membranes were represented as homogeneously charged plates located at the center of the phosphocholine headgroup. Accordingly, \(d_{\text{w}}\) was defined as \(d\) minus the headgroup-headgroup distance \(d_{\text{HB}}\) of DPPC for the description of the electrostatic interaction. Here, \(d_{\text{HB}} = 37.8\) Å was used according to the results of Kucerka et al. (36). The calculation of the repulsion between the two charged surfaces across the mixed electrolyte is presented in Text S2 in the Supporting Material.

**RESULTS AND DISCUSSION**

Fig. 3 shows the reciprocal space map of DPPC membrane multilayers doped with 25 mol % Le\(^X\) lipid measured at 60°C in Ca\(^{2+}\)-free buffer. The alignment of the membranes parallel to the substrate surface can be evidenced from the sharp central specular maximum along \(q_{||} = 0\), most prominently seen in the Γ-integrated Bragg sheet intensities (see Fig. 8, a and c).

**Lamellar periodicities of DPPC multilayers and the influence of Le\(^X\)**

Fig. 4 summarizes the influence of Le\(^X\) lipid on the equilibrium lamellar periodicity \(d\) in the absence and presence of
Ca$^{2+}$, calculated from the $q_z$-positions of the Bragg peaks in the scattering signals. As presented in the figure, Ca$^{2+}$ has a significant influence on the periodicity of pure DPPC membranes: $d = 66.1$ Å in the absence of Ca$^{2+}$, while $d = 90.0$ Å in the presence of 5 mM CaCl$_2$.

We found that the lamellar periodicity strongly depends on the molar fraction of Le$^X$ lipids. The incorporation of 2 mol % of Le$^X$ lipid already results in an increase in the periodicity in Ca$^{2+}$-free buffer (from $\approx 66$ Å to $\approx 74$ Å) and a sharp decrease in buffer containing 5 mM Ca$^{2+}$ (from $\approx 90$ Å to $\approx 83$ Å). This finding indicates that the opposing membranes are cross-linked by the trans-homophilic interactions between Le$^X$ headgroups even at a low surface density ($\approx 0.03$ Le$^X$ lipids per nm$^2$). According to

the increase in the molar fraction of Le$^X$ lipid up to 25 mol %, the periodicities in the presence and absence of Ca$^{2+}$ converge to a saturation level of $d_{Le^X} \approx 78$ Å (indicated with a dashed line in Fig. 4), which seems optimal for the formation of homophilic pairs that cross-link the membranes.

In fact, this periodicity is in good agreement with the sum of the thickness of the hydrocarbon chain region ($\approx 40$ Å) and the thickness of two saccharide headgroups ($\approx 2 \times 22$ Å = 44 Å), if one assumes a slight interdigitation of the opposing saccharide pairs. The convergence of the lamellar periodicities at all Ca$^{2+}$ concentrations according to an increase in molar fraction of Le$^X$ lipid can be attributed to a strengthening in membrane confinement around the optimal periodicity $d_{Le^X}$ as a result of an increased density of trans-homophilic Le$^X$ pairs.

**Intermembrane potential under external stress**

At low Ca$^{2+}$ concentrations, the lamellar periodicities of the pure DPPC membranes ($d \approx 68$ Å for 1 mM and $d \approx 69$ Å for 2 mM) are $\approx 10$ Å smaller than the saturation level ($d_{Le^X} \approx 78$ Å). Here, the increase in the periodicity with increasing Le$^X$ lipid fraction suggests that Le$^X$ pairs expand the membrane separation while they are subject to a compression force. In contrast, at a higher Ca$^{2+}$ concentration (5 mM), the incorporation of Le$^X$ lipids leads to a decrease in the periodicity: pure DPPC membranes exhibit a spacing of $d \approx 90$ Å, which is much larger than $d_{Le^X}$. Here, Le$^X$ pairs attract the opposing membranes against a tensile force. These findings indicate that experiments at various Ca$^{2+}$ concentrations offer a unique possibility to study the specific Le$^X$-Le$^X$ interaction under defined external stresses. The strength of these compressional and tensile stresses exerted under various buffer conditions is discussed in the following.

**Interactions between DPPC membranes**

At first, the interaction between pure DPPC membranes is quantified, which is necessary for the further investigation of the trans-homophilic interaction of Le$^X$ saccharide motifs. Although DPPC membranes are commonly studied model systems that have been characterized in detail (36), the comprehensive theoretical description of intermembrane interactions is still challenging (41). The interaction of electrically neutral DPPC membranes can be described as the sum of three force contributions (30)—vdW attraction, hydration repulsion, and undulation repulsion (see Materials and Methods). In Fig. 5a, the modeled interaction contributions are plotted as a function of the lamellar periodicity $d$. As can be seen, for low $d$-values corresponding to short membrane separations, the interaction is dominated by hydration repulsion, whereas vdw attraction is dominant at larger separations. Fig. 5b represents the absolute of
the modeled disjoining pressure $\Pi$ (i.e., the sum of all interaction contributions). $|\Pi|$ is zero at $d = 66.0$ Å, which corresponds to the equilibrium separation between DPPC membranes. This theoretically predicted equilibrium separation is in excellent agreement with the experimentally obtained lamellar periodicity of DPPC membranes in Ca$^{2+}$-free buffer, $d = 66.1$ Å.

Note that in pure H$_2$O, $d \approx 65$ Å is observed. As predicted by Petrache et al. (39), we found that the influence of NaCl is very weak ($\Delta d = 0.1$ Å for 100 mM NaCl). Therefore, this effect is neglected in the following considerations.

### Influence of Ca$^{2+}$ Ions on Interactions between DPPC membranes

As shown in Fig. 4, we observed a remarkable influence of Ca$^{2+}$ on the lamellar periodicities of DPPC membranes: the addition of 1 mM Ca$^{2+}$ already causes an increase in lamellar spacing by $\Delta d = 1.8$ Å ($d = 67.9$ Å). At 5 mM Ca$^{2+}$ the spacing is increased by as much as $\Delta d = 23.9$ Å ($d = 90.0$ Å). The summary of the effect of Ca$^{2+}$ on the periodicity is presented in Table 1.

To model the electrostatic repulsion caused by the adsorption of Ca$^{2+}$ ions at the membrane surfaces, we used the corresponding positive surface charge density $\sigma$ as a free model parameter to achieve the experimentally obtained $\Delta d$ values. Fig. 6 a shows the electrostatic repulsion required to match the experimentally determined $\Delta d$ values for 1, 2, and 5 mM CaCl$_2$. In the inset, the surface charge density $\sigma$ corresponding to each condition is given. Fig. 6 b represents the absolute of the net interactions calculated from the sum of all four interfacial forces. As a clear trend, an increase in the charge density with increasing Ca$^{2+}$ concentration is observed (from $\sigma = 39$ mC/m$^2$ at 1 mM to $\sigma = 84$ mC/m$^2$ at 5 mM; see Table 1). Within the model, the errors in $\sigma$ (±1 mC/m$^2$) solely result from the error in the determination of Bragg peak positions and the corresponding error in $\Delta d$ (±0.1 Å). Systematic errors introduced by the model, especially in the treatment of undulation forces, are more significant, but do not influence the obtained order of magnitude (see Materials and Methods).

For each Ca$^{2+}$ concentration, the number of DPPC molecules per adsorbed Ca$^{2+}$ ion was calculated from the charge densities by assuming that the area occupied by one DPPC molecule is 65 Å$^2$ (45). This enables us to calculate the affinity constant $K_a$ of the DPPC-Ca$^{2+}$ interaction (39),

$$K_a = \frac{[\text{DPPC} + \text{Ca}^{2+}]}{[[\text{DPPC}][\text{Ca}^{2+}]]},$$

where $[\text{DPPC} + \text{Ca}^{2+}]$ denotes the molar fraction of DPPC molecules that are associated with a Ca$^{2+}$ ion, $[\text{DPPC}]$ the molar fraction of free DPPC molecules, and $[[\text{Ca}^{2+}]]$ the bulk Ca$^{2+}$ concentration in M. The calculated values are summarized in Table 1. The binding affinities are quite weak, of the order of several M$^{-1}$. Furthermore, the affinity constant decreases with increasing Ca$^{2+}$ concentration. This tendency can be understood from the increase in $\sigma$ according to the increase in Ca$^{2+}$ concentrations, which would make the adsorption of further Ca$^{2+}$ electrostatically less favorable.

### Cross-linking the membranes: forces and energies

To estimate the forces and energies involved in the cross-linking of neighboring membranes by transhomophilic

**TABLE 1** Characteristics of DPPC membranes subject to various Ca$^{2+}$ concentrations: lamellar periodicities, charge densities, number of DPPC molecules per adsorbed Ca$^{2+}$, and affinity constants

<table>
<thead>
<tr>
<th>Ca$^{2+}$ concentration</th>
<th>$d$</th>
<th>$\Delta d$</th>
<th>Charge density $\sigma$</th>
<th>Number of DPPC molecules per Ca$^{2+}$</th>
<th>Affinity $K_a$</th>
</tr>
</thead>
<tbody>
<tr>
<td>0 mM</td>
<td>(66.1 ± 0.1) Å</td>
<td>0 Å</td>
<td>(39 ± 1) mC/m$^2$</td>
<td>—</td>
<td>(7.9 ± 0.2) M$^{-1}$</td>
</tr>
<tr>
<td>1 mM</td>
<td>(67.9 ± 0.1) Å</td>
<td>(1.8 ± 0.1) Å</td>
<td>(46 ± 1) mC/m$^2$</td>
<td>107 ± 2</td>
<td>(4.6 ± 0.1) M$^{-1}$</td>
</tr>
<tr>
<td>2 mM</td>
<td>(69.1 ± 0.1) Å</td>
<td>(3.0 ± 0.1) Å</td>
<td>(84 ± 1) mC/m$^2$</td>
<td>59 ± 1</td>
<td>(3.3 ± 0.1) M$^{-1}$</td>
</tr>
</tbody>
</table>

Within the chosen model, the errors in $\sigma$, number of DPPC, and $K_a$ follow solely from the error in $\Delta d$. 

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LeX-LeX interactions, DPPC membranes doped with 2 mol % LeX lipid at 5 mM CaCl2 are discussed in detail. Compared to the periodicity of pure DPPC membranes, the presence of 2 mol % LeX lipid causes a reduction in membrane periodicity from \( d_{0\%} = 90.0 \) Å to \( d_{2\%} = 83.0 \) Å. The value \( d_{0\%} \) denotes the lamellar spacing of DPPC membranes without LeX lipids and represents the electrostatic repulsion between the membranes at a given Ca\(^{2+}\) concentration. Here, LeX-LeX pairs attract the opposing membranes against tensile stress. Due to the low molar fraction of LeX lipid, the nonspecific intermembrane forces can be approximated by the disjoining pressure between pure DPPC membranes (solid curve, Fig. 7). To decrease the periodicity from \( d_{0\%} \) to \( d_{2\%} \), an additional pressure of \( \Delta \Pi_{2\%} \approx 350 \) Pa (indicated by an arrow in Fig. 7) is required. Moreover, the work required for this compression can be estimated by integrating the curve in Fig. 7 between \( d_{0\%} \) and \( d_{2\%} \) (shaded area in Fig. 7): \( \Delta U_{2\%} \approx 110 \) nJ/m\(^2\).

By assuming that all available LeX groups are involved in the cross-linking, the lowest required binding force \( F \) and binding energy \( E \) per molecular pair can be calculated from \( \Delta \Pi_{2\%} \) and \( \Delta U_{2\%} \) multiplied by the mean area per LeX group (65 Å\(^2\)/0.02 Å\(^2\) = 3250 Å\(^2\)): \( F \approx 10 \) fN and \( E \approx 10^{-3} k_B T \), respectively. However, it is likely that not all LeX lipids but rather a small fraction are involved in the formation of pairs, and thus typical forces and energies per formed pair are significantly higher. In fact, the binding energy and force of individual LeX pairs estimated from AFM experiments and molecular dynamics simulation are of the order of several \( k_B T \) and 10 pN, respectively (5,46). Thus, even low densities of membrane-anchored LeX (corresponding to one LeX motif per thousands of square nanometers) should be sufficient for the cross-linking of membranes at calcium concentrations used in this study.

### Influence of LeX on the mechanics of interacting membranes

The mechanical properties of the interacting membranes (characterized by the membrane bending modulus \( \kappa \) and the vertical compression modulus \( B \)) can be calculated from the off-specular scattering signals. Fig. 2 (right) shows the measured (a) and the simulated (b) intensity of a typical second Bragg sheet. Because effects of refraction and absorption, which are not considered in kinematic approximation, become important in the vicinity of the sample horizons (Yoneda wings) at \( \Omega = 0 \) and \( \Gamma - \Omega = 0 \), this angular region (indicated with dashed lines in the figure) was excluded from the comparison.

To highlight the influence of trans-homophilic LeX pairs on the membrane mechanics, we compared membranes with 10 mol % and 25 mol % LeX lipid in Ca\(^{2+}\)-free buffer that exhibit lamellar periodicities very close to the saturation value of \( d_{LeX} \approx 78 \) Å (see Fig. 4). Thus, differences in the obtained mechanical parameters can be directly related to the different lateral densities of LeX lipid molecules but not to a difference in equilibrium membrane periodicity. Fig. 8 shows the comparison of the measured and modeled scattering signals from membranes with 10 mol % (Fig. 8, a and b) and 25 mol % (Fig. 8, c and d) LeX lipid in two characteristic representations. The sheet intensities integrated along \( \Gamma \) plotted as a function of \( q || \) (Fig. 8, a and c) represent the displacement self-correlation function of an average membrane in the solid-supported stack, whereas the pressure represent the resulting change \( \Delta d \) in equilibrium lamellar periodicity.

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**Note:** The provided text contains some mathematical expressions and diagrams that are represented using symbols and figures. The exact mathematical content and diagram details are not transcribed here but are integral to the understanding of the original text. The focus is on the descriptive content rather than the formatted figures and symbols.
the widths of the sheets along $\Gamma$ plotted as a function of $q_\parallel$ (Fig. 8, b and d) represent the de Gennes parameter $\lambda(20)$ independent of the other parameters.

Due to the close relation between $G$ and $q_\perp z$, this is valid not only for the $q_\perp z$-integrated intensity and the $q_\perp z$-width of the Bragg sheets, but also for the $G$-integrated intensity and the $G$-width, in good approximation. The modeled signals (solid lines) corresponding to the best matching parameters are superimposed onto the experimental data points. Here, the thick (0.1 mm) layer of H2O buffers in the liquid cell leads to incoherent scattering by $^1$H and results in a high absorption of the neutron beam in the transmission regime.

Therefore, the reflection regimes ($\Omega > 0$ and $\Gamma - \Omega > 0$) between the vertical dashed lines in Fig. 8, a and c, were used for the comparison. Another feature of the scattering signals not captured by the models is the existence of satellite peaks (indicated in Fig. 8 c, but also seen in Fig. 8 a and Fig. 3). From their position in $q_\perp z$ and $q_\parallel$, they were identified as results of double-scattering processes (see Text S3 and Fig. S3 in the Supporting Material). Therefore, experimental and modeled signals are not compared in the close vicinity of the satellite peaks. As presented in the figure, the models are in excellent agreement with the experimental data within the analyzed range. It should be noted that the almost perfect matching of the sheet widths (Fig. 8, b and d) enables the precise experimental determination of the de Gennes parameter $\lambda$ ($\Delta \lambda/\lambda < 10\%$) and the Caillé parameter $\eta$ ($\Delta \eta/\eta < 10\%$). This leads to a high accuracy in the calculation of the mechanical parameters $\kappa$ and $B$ ($\Delta \kappa/\kappa < 20\%$, $\Delta B/B < 20\%$). The dips at $q_\parallel \approx 0$ in Fig. 8, b and d, in both experiment and model are result of the distorted shape of the Bragg sheets around their intersection with the specular axis.

The best-matching model parameters are summarized in Table 2. The cut-off radii $R$ are in the range of 1 $\mu m$, consistent with those found for other membrane multilayer systems (22,23). Interestingly, the bending rigidities obtained for 10 mol % ($\kappa \approx 16 k_B T$) and 25 mol % ($\kappa \approx 17 k_B T$) are identical to that of pure DPPC membranes,

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**TABLE 2** Parameters of the best matching models for DPPC membrane multilayers doped with 10 mol % and 25 mol % LeX lipid at 60 $^\circ$C in Ca$^{2+}$-free buffer

<table>
<thead>
<tr>
<th>LeX lipid fraction</th>
<th>$\eta$ [Å]</th>
<th>$\lambda$ [Å]</th>
<th>$R$ [$\mu$m]</th>
<th>$\kappa$ [$k_B T$]</th>
<th>$B$ [MPa]</th>
</tr>
</thead>
<tbody>
<tr>
<td>10 mol %</td>
<td>0.085 ± 0.005</td>
<td>65 ± 5</td>
<td>0.8 ± 0.1</td>
<td>16 ± 3</td>
<td>0.22 ± 0.05</td>
</tr>
<tr>
<td>25 mol %</td>
<td>0.046 ± 0.005</td>
<td>38 ± 5</td>
<td>0.7 ± 0.1</td>
<td>17 ± 3</td>
<td>0.7 ± 0.1</td>
</tr>
</tbody>
</table>

The addition of 5 mM Ca$^{2+}$ did not significantly alter the obtained parameters. Errors in $\kappa$ and $B$ follow from the errors in $\eta$ and $\lambda$. 

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k ≈ 18 k_BT (Fig. S1 and Table S1) within the error. This indicates that the membrane-anchored oligosaccharides do not significantly contribute to the membrane bending rigidity even at the highest LeX lipid density used in this study (25 mol %, corresponding to a lateral density of 0.3 saccharide headgroups per nm²).

On the other hand, the compression moduli obtained for 10 mol % (B = 0.22 MPa) and 25 mol % (B = 0.70 MPa) show a clear difference: The higher density of LeX motifs results in a much stronger confinement of the membranes between their neighbors. This finding can be interpreted as result of the cross-linking of the membranes via trans-homophilic LeX pairs, which is strengthened according to an increase in the number of cross-linkers.

The addition of 5 mM Ca²⁺ did not have a significant influence on the off-specular scattering intensity and thus on the obtained parameters of the continuum mechanical model (see Fig. S2). Although the intermembrane water layer is ≈ 40 Å thick in the studied systems, the observed compression moduli are still comparable to those of pure phospholipid membranes with much thinner water layers (<20 Å), where the values were found to decay rapidly with increasing water layer thickness (47). This finding highlights the substantial stiffening achieved by the cross-linkers.

**Influence of Ca²⁺ on membrane adhesion**

As presented in Fig. 4, the lamellar periodicities in the presence and absence of Ca²⁺ converge to a saturation value (d_{LeX} ≈ 78 Å) according to the increase in the molar fraction of LeX lipids toward the physiological level of glycolipids in eukaryotic membranes (>10 mol %) (48). The observed tendency suggests that the molar fraction of LeX lipids significantly influences the membrane adhesion via homophilic saccharide-saccharide interactions, but the presence of Ca²⁺ does not seem to be crucial. From the analysis of the off-specular scattering signals, we also found that both bending rigidity and compression modulus of the membranes were not influenced by the presence of Ca²⁺.

To date, it has commonly been assumed that divalent cations, preferably Ca²⁺, are prerequisite for homophilic LeX-LeX interactions (8,9,25,49). In contrast to these results, there have been several experimental studies reporting that homophilic LeX interaction can occur even in the absence of Ca²⁺. For example, AFM experiments suggested that the presence of Ca²⁺ does not contribute significantly to the binding forces (5). Nishimura et al. (50) and Su et al. (51) observed LeX aggregates in the absence of Ca²⁺ by time-of-flight mass spectroscopy and molecular beam spectroscopy, respectively. Moreover, using molecular dynamics simulations, Gourmala et al. (46) reported that the LeX dimer is stable both in the presence and absence of Ca²⁺, but that the interactions are strengthened by Ca²⁺. Although neutron scattering is not sensitive to the individual molecular interactions, the formation of trans-homophilic LeX pairs suggested by our experiments is in good agreement with these reports.

**CONCLUSIONS**

Stacks of membranes doped with LeX lipids on solid substrates were used for the study of membrane adhesion via specific carbohydrate-carbohydrate interactions. Specular and off-specular neutron scattering provided quantitative insights into the influence of surface density of LeX motifs and Ca²⁺ concentration on the structure and mechanics of interacting membranes. The obtained results demonstrate that neighboring membranes are tightly confined by even a low density of carbohydrate cross-linkers.

In comparison to the significant influence of the surface density (molar ratio) of LeX motifs, we found that Ca²⁺ does not significantly affect the formation of trans-homophilic pairs. The approach is promising for a systematic investigation of the membrane adhesion mediated via weak, but specific carbohydrate-carbohydrate interactions.

**SUPPORTING MATERIAL**

Additional text, three figures, and one table are available at http://www.biophysj.org/biophysj/supplemental/S0006-3495(11)00321-3.

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**REFERENCES**


